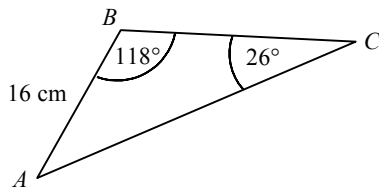
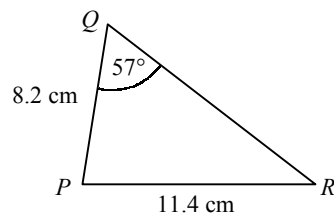


1



The diagram shows triangle ABC in which $AB = 16$ cm, $\angle ABC = 118^\circ$ and $\angle ACB = 26^\circ$.
Use the sine rule to find the length AC to 3 significant figures.

2

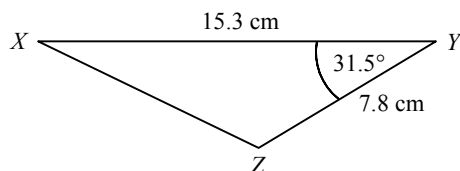


The diagram shows triangle PQR in which $PQ = 8.2$ cm, $PR = 11.4$ cm and $\angle PQR = 57^\circ$.
Use the sine rule to find the size of $\angle PRQ$ in degrees to 1 decimal place.

3

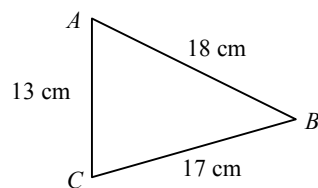
In triangle ABC , $AB = 16.2$ cm, $BC = 12.3$ cm and $\angle BAC = 37^\circ$.
Find the two possible sizes of $\angle ACB$ and the corresponding lengths of AC .

4



The diagram shows triangle XYZ in which $XY = 15.3$ cm, $YZ = 7.8$ cm and $\angle XYZ = 31.5^\circ$.
Use the cosine rule to find the length XZ .

5

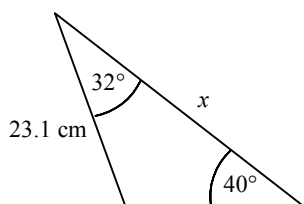


The diagram shows triangle ABC in which $AB = 18$ cm, $AC = 13$ cm and $BC = 17$ cm.
Use the cosine rule to find the size of $\angle ACB$.

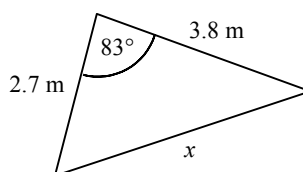
6

Find the length x in each triangle.

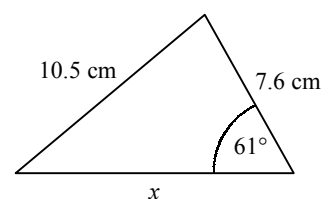
a



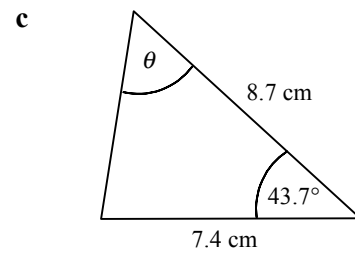
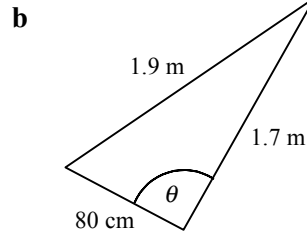
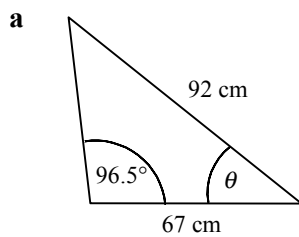
b



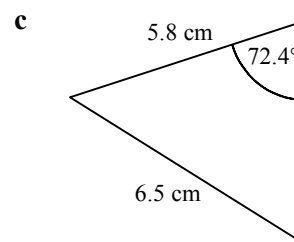
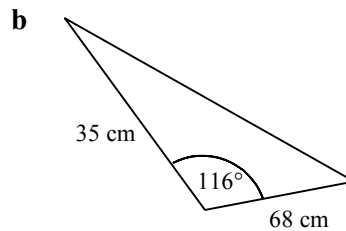
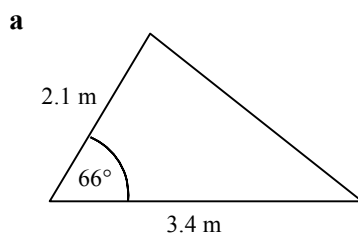
c



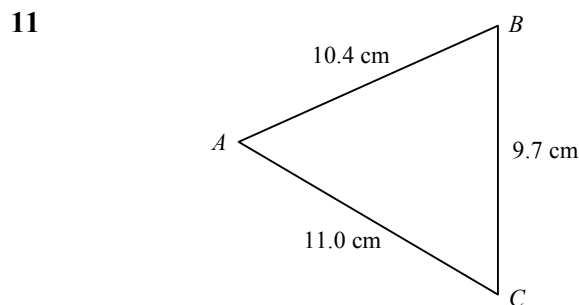
- 7 Find the angle θ in each triangle.



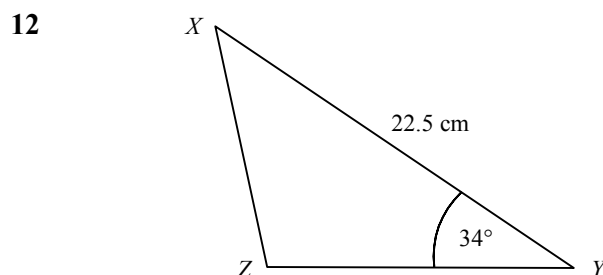
- 8 Find the area of each of the following triangles.



- 9 Joanne walks 4.2 miles on a bearing of 138° . She then walks 7.8 miles on a bearing of 251° .
- a** Calculate how far Joanne is from the point where she started.
- b** Find, as a bearing, the direction in which Joanne would have to walk in order to return to the point where she started.
- 10 A ferry and a cargo ship are both approaching the same port. The ferry is 3.2 km from the port on a bearing of 076° and the cargo ship is 6.9 km from the port on a bearing of 323° . Find the distance between the two vessels and the bearing of the cargo ship from the ferry.

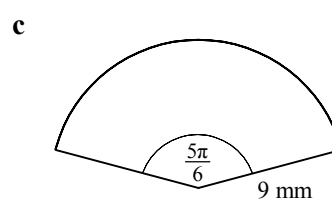
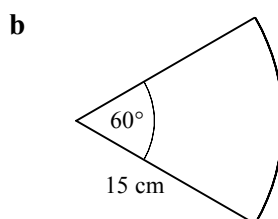
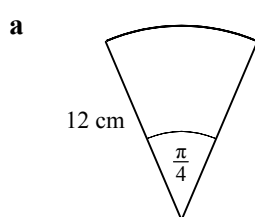


The diagram shows triangle ABC in which $AB = 10.4$ cm, $AC = 11.0$ cm and $BC = 9.7$ cm. Find the area of the triangle to 3 significant figures.

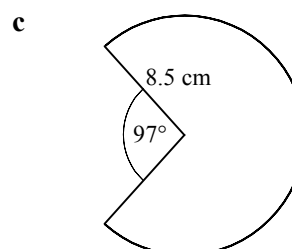
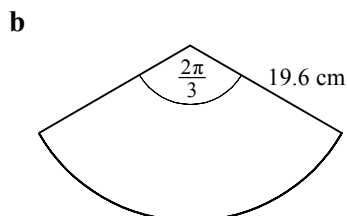
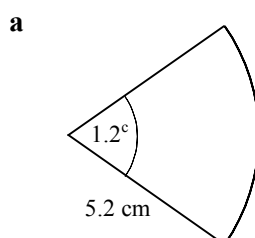


The diagram shows triangle XYZ in which $XY = 22.5$ cm and $\angle XYZ = 34^\circ$. Given that the area of the triangle is 100 cm^2 , find the length XZ .

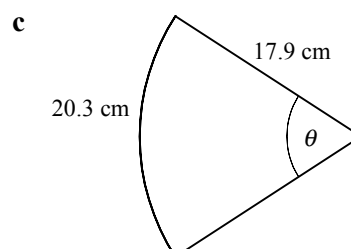
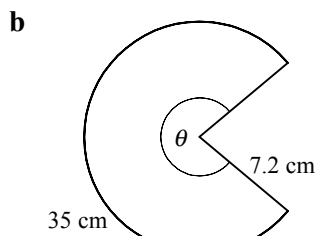
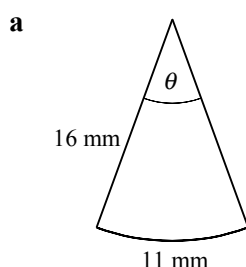
- 1 Convert each angle from degrees to radians, giving your answers in terms of π .
- a 180° b 30° c 45° d 720° e 18° f 120°
g 15° h 40° i 270° j 7.5° k 144° l 220°
- 2 Convert each angle from degrees to radians, giving your answers to 2 decimal places.
- a 10° b 38° c 291° d 63.8° e 507° f 126.2°
- 3 Convert each angle from radians to degrees.
- a 2π b $\frac{\pi}{3}$ c $\frac{\pi}{2}$ d $\frac{3\pi}{4}$ e $\frac{\pi}{18}$ f $\frac{\pi}{30}$
g $\frac{5\pi}{6}$ h $\frac{\pi}{8}$ i 3π j $\frac{2\pi}{15}$ k $\frac{7\pi}{3}$ l $\frac{9\pi}{20}$
- 4 Convert each angle from radians to degrees, giving your answers to 1 decimal place.
- a 2° b 0.5° c 3.1° d 1.43° e 8.7° f 0.742°
- 5 Find, in terms of π , the length of the arc in each of the following circular sectors.



- 6 Find, to 3 significant figures, the perimeter of each of the following circular sectors.



- 7 Find, in radians to 2 decimal places, the angle θ in each of the following circular sectors.



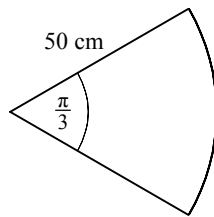
- 8 The minor arc AB of a circle, centre O , has length 46.2 cm.

Given that $\angle AOB = 78.5^\circ$, find

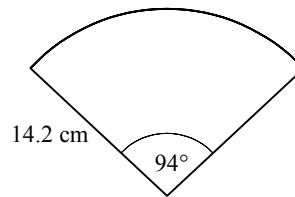
- a the distance OA , b the perimeter of sector OAB .

- 9 Find, in cm^2 to 1 decimal place, the area of each of the following circular sectors.

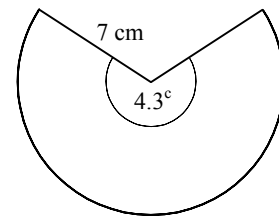
a



b



c

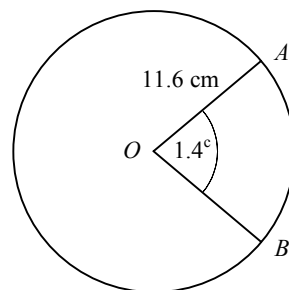


- 10 PQ is an arc of a circle of radius 8 cm, centre O .

Given that arc PQ has length 12 cm, find

- a the angle, in radians, subtended by PQ at O ,
b the area of sector OPQ .

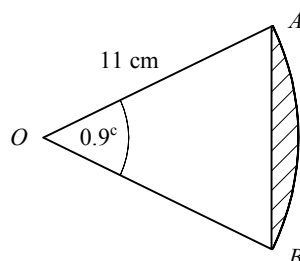
11



The diagram shows a circle of radius 11.6 cm, centre O . The arc of the circle AB subtends an angle of 1.4 radians at O . Find, to 3 significant figures,

- a the perimeter of the minor sector OAB , b the perimeter of the major sector OAB ,
c the area of the minor sector OAB , d the area of the major sector OAB .

12

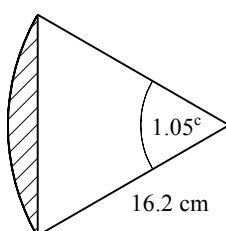


The diagram shows a circular sector OAB . Find the area of

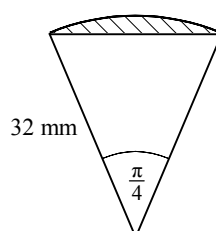
- a the sector OAB , b the triangle OAB , c the shaded segment.

- 13 Find the area of the shaded segment in each of the following circular sectors.

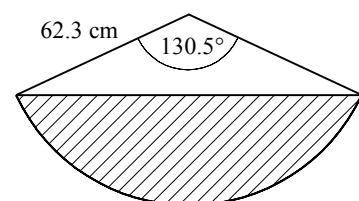
a



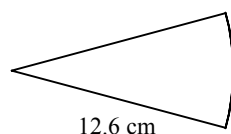
b



c

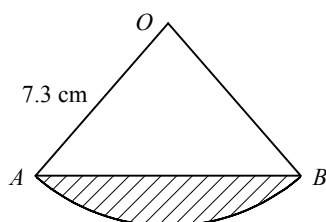


1



The diagram shows a sector of a circle of radius 12.6 cm.
Given that the perimeter of the sector is 31.7 cm, find its area.

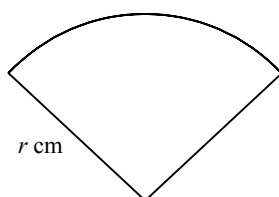
2



The diagram shows a sector OAB of a circle, centre O and radius 7.3 cm.
Given that the area of the sector is 38.4 cm^2 , find

- the size of $\angle AOB$ in radians,
- the perimeter of the shaded segment.

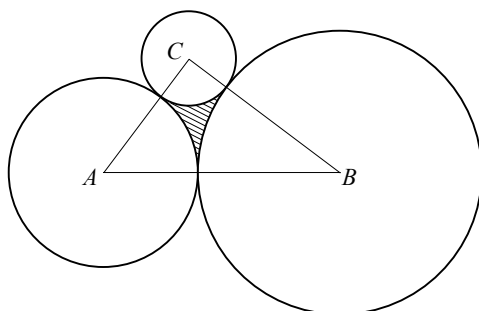
3



The diagram shows a sector of a circle of radius $r \text{ cm}$. The area of the sector is 40 cm^2 .

- Show that the perimeter of the sector is $(2r + \frac{80}{r}) \text{ cm}$.
- Hence find the set of values of r for which the perimeter of the sector is less than 26 cm.

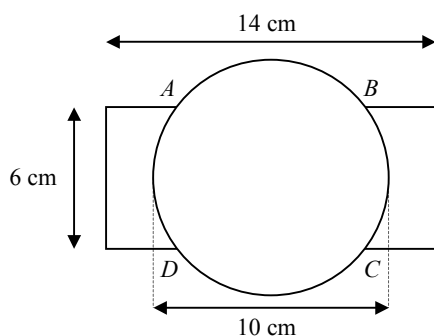
4



The diagram shows three circles with centres A , B and C , and radii 4 cm, 6 cm and 2 cm respectively. Each circle touches the other two circles.

- Prove that triangle ABC is a right-angled triangle.
- Find $\angle ABC$ in radians to 2 decimal places.
- Show that the area of the shaded region enclosed by the three circles is 1.86 cm^2 to 3 significant figures.

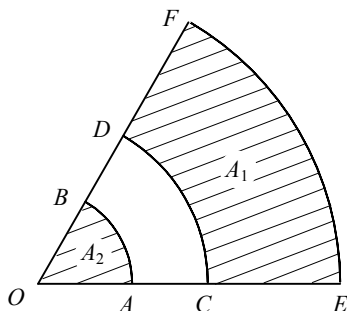
5



The diagram shows a company logo which consists of a circle of diameter 10 cm drawn on top of a rectangle measuring 6 cm by 14 cm. The centres of the circle and rectangle are coincident and the two shapes intersect at A , B , C and D .

- Find the length of the chord of the circle AB .
- Show that the perimeter of the logo is 42.5 cm to 3 significant figures.
- Find the area of the logo.

6



AB , CD and EF are arcs of concentric circles, centre O , such that $OACE$ and $OBDF$ are straight lines as shown in the diagram. The area of the shaded region $CEFD$ is denoted by A_1 and the area of the shaded sector OAB by A_2 .

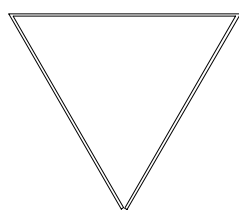
Given that $OA = r$ cm, $AC = 2$ cm, $OE = 8$ cm and $\angle AOB = \theta$ radians,

- find an expression for A_1 in terms of r and θ .

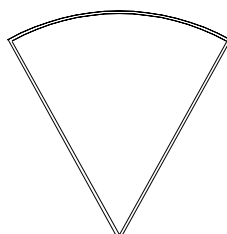
Given also that $A_1 = 7A_2$,

- show that $r = 2.5$

7



Shape A



Shape B

A girl is playing with a paper clip. She straightens the wire and then bends it to form an equilateral triangle, *Shape A* above. She then curves one side of the triangle to form a sector of a circle, *Shape B* above.

Find, to 1 decimal place, the percentage change in the area enclosed by the paper clip when it is changed from *Shape A* to *Shape B*, indicating whether this is an increase or decrease.

1 Find to 3 decimal places the value of

a $\sin 131^\circ$

b $\tan 340.5^\circ$

c $\cos 418^\circ$

d $\sin(-165.2^\circ)$

2 Give the exact value of

a $\cos 60^\circ$

b $\sin 45^\circ$

c $\tan 45^\circ$

d $\cos 30^\circ$

e $\sin 90^\circ$

f $\tan 30^\circ$

g $\cos 120^\circ$

h $\sin 135^\circ$

i $\tan 210^\circ$

j $\cos 225^\circ$

k $\sin 300^\circ$

l $\tan 120^\circ$

m $\cos 330^\circ$

n $\tan 150^\circ$

o $\cos(-60^\circ)$

p $\sin 405^\circ$

q $\tan(-45^\circ)$

r $\sin(-240^\circ)$

s $\tan 570^\circ$

t $\cos(-150^\circ)$

3 Find to 3 decimal places the value of

a $\cos 0.42^\circ$

b $\sin 4.16^\circ$

c $\tan(-3.1^\circ)$

d $\cos 11.25^\circ$

4 Give the exact value of

a $\sin \frac{\pi}{6}$

b $\cos \frac{\pi}{2}$

c $\sin \frac{\pi}{4}$

d $\tan \frac{\pi}{3}$

e $\cos \frac{\pi}{3}$

f $\sin \frac{2\pi}{3}$

g $\tan \frac{3\pi}{4}$

h $\cos \frac{5\pi}{6}$

i $\tan \frac{5\pi}{3}$

j $\cos \frac{5\pi}{4}$

k $\sin(-\frac{\pi}{6})$

l $\tan(-\frac{5\pi}{6})$

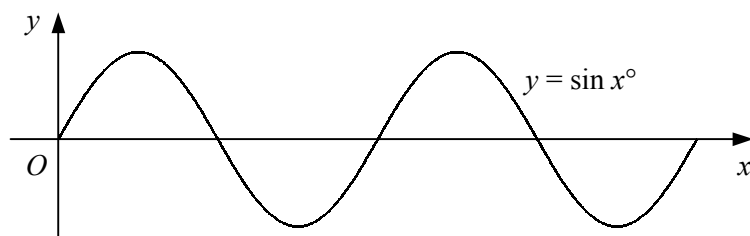
m $\sin 3\pi$

n $\tan(-\frac{5\pi}{4})$

o $\cos \frac{8\pi}{3}$

p $\sin(-\frac{7\pi}{3})$

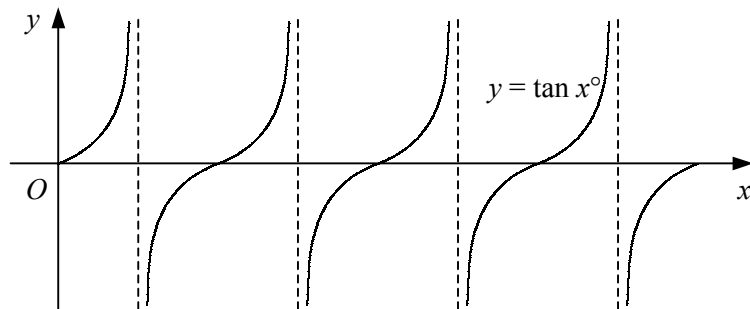
5



The graph shows the curve $y = \sin x^\circ$ in the interval $0 \leq x \leq 720$.

- Write down the coordinates of any points where the curve intersects the coordinate axes.
- Write down the coordinates of the turning points of the curve.

6



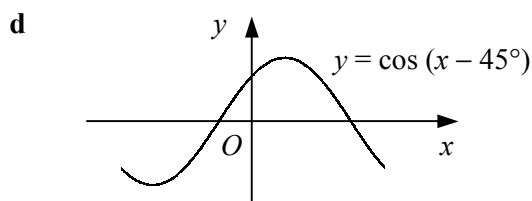
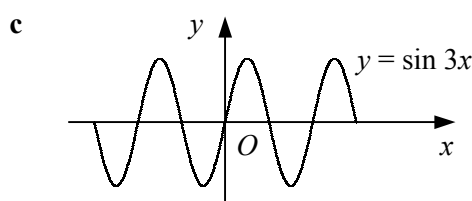
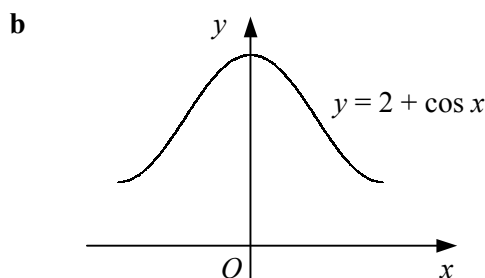
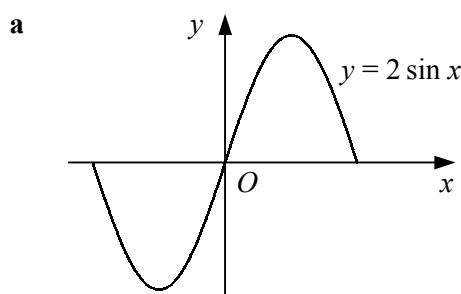
The graph shows the curve $y = \tan x^\circ$ in the interval $0 \leq x \leq 720$.

- Write down the coordinates of any points where the curve intersects the coordinate axes.
- Write down the equations of the asymptotes.

- 7 Describe the transformation that maps the graph of $y = \sin x^\circ$ onto the graph of
a $y = 3 \sin x^\circ$ **b** $y = \sin 4x^\circ$ **c** $y = \sin (x + 60)^\circ$ **d** $y = \sin (-x^\circ)$
- 8 Sketch each of the following pairs of curves on the same set of axes in the interval $0 \leq x \leq 360^\circ$.
a $y = \cos x$ and $y = 3 \cos x$ **b** $y = \sin x$ and $y = \sin (x - 30^\circ)$
c $y = \cos x$ and $y = \cos 2x$ **d** $y = \tan x$ and $y = 2 + \tan x$
e $y = \sin x$ and $y = -\sin x$ **f** $y = \cos x$ and $y = \cos (x + 60^\circ)$
g $y = \tan x$ and $y = \tan \frac{1}{2}x$ **h** $y = \sin x$ and $y = 1 + \sin x$

- 9 Each curve is shown for the interval $-180^\circ \leq x \leq 180^\circ$.

Write down the coordinates of the turning points of each curve in this interval.



- 10 Write down the period of each of the following graphs.

- a** $y = \sin x^\circ$ **b** $y = \tan x^\circ$ **c** $y = 2 \cos x^\circ$
d $y = \sin 2x^\circ$ **e** $y = \tan (x + 30)^\circ$ **f** $y = \cos \frac{1}{3}x^\circ$

- 11 Sketch each of the following curves for x in the interval $0 \leq x \leq 360$. Show the coordinates of any points of intersection with the coordinate axes and the equations of any asymptotes.

- a** $y = \tan x^\circ$ **b** $y = \cos (x + 30)^\circ$ **c** $y = \sin 2x^\circ$
d $y = 1 + \cos x^\circ$ **e** $y = \sin \frac{1}{2}x^\circ$ **f** $y = \tan (x + 90)^\circ$
g $y = \sin (x - 45)^\circ$ **h** $y = -\tan x^\circ$ **i** $y = \cos (x - 120)^\circ$

- 12 Sketch each of the following curves for x in the interval $0 \leq x \leq 2\pi$. Show the coordinates of any turning points and the equations of any asymptotes.

- a** $y = \cos x$ **b** $y = 3 \sin x$ **c** $y = \tan 2x$
d $y = \sin (x - \frac{\pi}{3})$ **e** $y = \cos \frac{1}{3}x$ **f** $y = \sin x - 2$
g $y = \tan (x + \frac{\pi}{4})$ **h** $y = \sin \frac{3}{4}x$ **i** $y = \cos (x - \frac{\pi}{6})$

- 1 Find all values of x in the interval $0 \leq x \leq 360^\circ$ such that
- a $\sin x = \frac{1}{2}$ b $\tan x = \sqrt{3}$ c $\cos x = 0$ d $\sin x = -1$
- e $\cos x = \frac{\sqrt{3}}{2}$ f $\sin x = \frac{1}{\sqrt{2}}$ g $\tan x = -1$ h $\cos x = -\frac{1}{2}$
- i $\sin x = -\frac{\sqrt{3}}{2}$ j $\tan x = \frac{1}{\sqrt{3}}$ k $\cos x = -\frac{1}{\sqrt{2}}$ l $\tan x = -\sqrt{3}$
- 2 Solve each equation for θ in the interval $0 \leq \theta \leq 360^\circ$ giving your answers to 1 decimal place.
- a $\cos \theta = 0.4$ b $\sin \theta = 0.27$ c $\tan \theta = 1.6$ d $\sin \theta = 0.813$
- e $\tan \theta = 0.1$ f $\cos \theta = 0.185$ g $\sin \theta = -0.6$ h $\tan \theta = -0.7$
- i $\cos \theta = -0.39$ j $\tan \theta = -3.4$ k $\cos \theta = -0.636$ l $\sin \theta = -0.203$
- 3 Solve each equation for x in the interval $0 \leq x \leq 360$.
Give your answers to 1 decimal place where appropriate.
- a $\sin(x - 60)^\circ = 0.5$ b $\tan(x + 30)^\circ = 1$ c $\cos(x - 45)^\circ = 0.2$
- d $\tan(x + 30)^\circ = 0.78$ e $\cos(x + 45)^\circ = -0.5$ f $\sin(x - 60)^\circ = -0.89$
- g $\cos(x + 45)^\circ = 0.9$ h $\sin(x + 30)^\circ = 0.14$ i $\cos(x - 60)^\circ = 0.6$
- j $\sin(x - 30)^\circ = -0.3$ k $\tan(x - 60)^\circ = -1.26$ l $\sin 2x^\circ = 0.5$
- m $\cos 2x^\circ = 0.64$ n $\sin 2x^\circ = -0.18$ o $\tan 2x^\circ = -2.74$
- p $\sin \frac{1}{2}x^\circ = 0.703$ q $\tan 3x^\circ = 0.591$ r $\cos 2x^\circ = -0.415$
- 4 Solve each equation for x in the interval $0 \leq x \leq 2\pi$ giving your answers in terms of π .
- a $\sin x = 0$ b $\cos x = \frac{1}{2}$ c $\tan x = 1$
- d $\cos x = -1$ e $\tan x = -\frac{1}{\sqrt{3}}$ f $\sin x = -\frac{1}{\sqrt{2}}$
- g $\tan(x + \frac{\pi}{6}) = \sqrt{3}$ h $\sin(x - \frac{\pi}{4}) = \frac{1}{2}$ i $\cos(x + \frac{\pi}{3}) = -\frac{\sqrt{3}}{2}$
- j $\sin(x + \frac{\pi}{3}) = \frac{1}{\sqrt{2}}$ k $\cos 2x = -\frac{1}{\sqrt{2}}$ l $\tan 3x = \frac{1}{\sqrt{3}}$
- 5 Solve each equation for θ in the interval $-180^\circ \leq \theta \leq 180^\circ$.
Give your answers to 1 decimal place where appropriate.
- a $\cos \theta = 0$ b $\tan 2\theta + 1 = 0$ c $\sin(\theta + 60^\circ) = 0.291$
- d $2 \tan(\theta - 15^\circ) = 3.7$ e $\sin 2\theta - 0.3 = 0$ f $4 \cos 3\theta = 2$
- g $1 + \sin(\theta + 110^\circ) = 0$ h $5 \cos(\theta - 27^\circ) = 3$ i $7 - 3 \tan \theta = 0$
- j $3 + 8 \cos 2\theta = 0$ k $2 + 6 \tan(\theta + 92^\circ) = 0$ l $1 - 4 \sin \frac{1}{3}\theta = 0$

- 6 Solve each equation for x in the interval $0 \leq x \leq 180^\circ$.

Give your answers to 1 decimal place where appropriate.

a $\tan(2x + 30^\circ) = 1$	b $\sin(2x - 15^\circ) = 0$	c $\cos(2x + 70^\circ) = 0.5$
d $\sin(2x + 210^\circ) = 0.26$	e $\cos(2x - 38^\circ) = -0.64$	f $\tan(2x - 56^\circ) = -0.32$
g $\cos(3x - 24^\circ) = 0.733$	h $\tan(3x + 60^\circ) = -1.9$	i $\sin(\frac{1}{2}x + 18^\circ) = 0.572$

- 7 Solve each equation for x in the interval $0 \leq x \leq 2\pi$, giving your answers to 2 decimal places.

a $\tan x = 0.52$	b $\cos 2x = 0.315$	c $\sin(x + \frac{\pi}{4}) = 0.7$
d $3 \cos x + 1 = 0$	e $\sin \frac{1}{2}x = 0.09$	f $\tan 2x = -0.225$
g $3 - 4 \sin(x - \frac{\pi}{3}) = 0$	h $\tan(2x + \frac{\pi}{6}) = 2$	i $\cos 3x = -0.81$
j $5 + 3 \tan x = 0$	k $\cos(2x - \frac{\pi}{2}) = -0.34$	l $1 + 6 \sin 2x = 0$

- 8 **a** Solve the equation

$$2y^2 - 3y + 1 = 0.$$

- b** Hence, find the values of x in the interval $0 \leq x \leq 360^\circ$ for which

$$2 \sin^2 x - 3 \sin x + 1 = 0.$$

- 9 Solve each equation for θ in the interval $0 \leq \theta \leq 360$.

Give your answers to 1 decimal place where appropriate.

a $\sin^2 \theta^\circ = 0.75$	b $1 - \tan^2 \theta^\circ = 0$
c $2 \cos^2 \theta^\circ + \cos \theta^\circ = 0$	d $\sin \theta^\circ(4 \cos \theta^\circ - 1) = 0$
e $4 \sin \theta^\circ = \sin \theta^\circ \tan \theta^\circ$	f $(2 \cos \theta^\circ - 1)(\cos \theta^\circ + 1) = 0$
g $\tan^2 \theta^\circ - 3 \tan \theta^\circ + 2 = 0$	h $3 \sin^2 \theta^\circ - 7 \sin \theta^\circ + 2 = 0$
i $\tan^2 \theta^\circ - \tan \theta^\circ = 6$	j $6 \cos^2 \theta^\circ - \cos \theta^\circ - 2 = 0$
k $4 \sin^2 \theta^\circ + 3 = 8 \sin \theta^\circ$	l $\cos^2 \theta^\circ + 2 \cos \theta^\circ - 1 = 0$
m $\tan^2 \theta^\circ + 3 \tan \theta^\circ - 1 = 0$	n $3 \sin^2 \theta^\circ + \sin \theta^\circ = 1$

- 10 **a** Sketch the curve $y = \cos x^\circ$ for x in the interval $0 \leq x \leq 360$.

- b** Sketch on the same diagram the curve $y = \cos(x + 90)^\circ$ for x in the interval $0 \leq x \leq 360$.

- c** Using your diagram, find all values of x in the interval $0 \leq x \leq 360$ for which

$$\cos x^\circ = \cos(x + 90)^\circ.$$

- 11 **a** Sketch the curves $y = \cos x^\circ$ and $y = \cos 3x^\circ$ on the same set of axes for x in the interval $0 \leq x \leq 360$.

- b** Solve, for x in the interval $0 \leq x \leq 360$, the equation

$$\cos x^\circ = \cos 3x^\circ.$$

- c** Hence solve, for x in the interval $0 \leq x \leq 180$, the equation

$$\cos 2x^\circ = \cos 6x^\circ.$$

- 1 a Given that $4 \sin x + \cos x = 0$, show that $\tan x = -\frac{1}{4}$.
 b Hence, find the values of x in the interval $0 \leq x \leq 360^\circ$ for which

$$4 \sin x + \cos x = 0,$$
 giving your answers to 1 decimal place.
- 2 a Show that

$$5 \sin^2 x + 5 \sin x + 4 \cos^2 x \equiv \sin^2 x + 5 \sin x + 4.$$
 b Hence, find the values of x in the interval $0 \leq x \leq 360^\circ$ for which

$$5 \sin^2 x + 5 \sin x + 4 \cos^2 x = 0$$
- 3 Solve each equation for x in the interval $0 \leq x \leq 360^\circ$.
 Give your answers to 1 decimal place where appropriate.
- | | |
|--|--|
| a $2 \sin x - \cos x = 0$ | b $3 \sin x = 4 \cos x$ |
| c $\cos^2 x + 3 \sin x - 3 = 0$ | d $3 \cos^2 x - \sin^2 x = 2$ |
| e $2 \sin^2 x + 3 \cos x = 3$ | f $3 \cos^2 x = 5(1 - \sin x)$ |
| g $3 \sin x \tan x = 8$ | h $\cos x = 3 \tan x$ |
| i $3 \sin^2 x - 5 \cos x + 2 \cos^2 x = 0$ | j $2 \sin^2 x + 7 \sin x - 2 \cos^2 x = 0$ |
| k $3 \sin x - 2 \tan x = 0$ | l $\sin^2 x - 9 \cos x - \cos^2 x = 5$ |
- 4 Solve each equation for θ in the interval $-\pi \leq \theta \leq \pi$ giving your answers in terms of π .
- | | |
|---|---|
| a $4 \cos^2 \theta = 1$ | b $4 \sin^2 \theta + 4 \sin \theta + 1 = 0$ |
| c $\cos^2 \theta + 2 \cos \theta - 3 = 0$ | d $3 \sin^2 \theta - \cos^2 \theta = 0$ |
| e $4 \sin^2 \theta - 5 \sin \theta + 2 \cos^2 \theta = 0$ | f $\sin^2 \theta - 3 \cos \theta - \cos^2 \theta = 2$ |
- 5 Prove that
- | | |
|--|---|
| a $(\sin x + \cos x)^2 \equiv 1 + 2 \sin x \cos x$ | b $\frac{1}{\cos x} - \cos x \equiv \sin x \tan x, \cos x \neq 0$ |
| c $\frac{\cos^2 x}{1 - \sin x} \equiv 1 + \sin x, \sin x \neq 1$ | d $\frac{1 + \sin x}{\cos x} \equiv \frac{\cos x}{1 - \sin x}, \cos x \neq 0$ |
- 6 a Prove the identity

$$(\cos x - \tan x)^2 + (\sin x + 1)^2 \equiv 2 + \tan^2 x.$$
 b Hence find, in terms of π , the values of x in the interval $0 \leq x \leq 2\pi$ such that

$$(\cos x - \tan x)^2 + (\sin x + 1)^2 = 3.$$
- 7 $f(x) \equiv \cos^2 x + 2 \sin x, 0 \leq x \leq 2\pi.$
- a Prove that $f(x)$ can be expressed in the form

$$f(x) = 2 - (\sin x - 1)^2.$$
- b Hence deduce the maximum value of $f(x)$ and the value of x for which this occurs.

- 1 Find, in terms of π , the values of x in the interval $0 \leq x \leq 2\pi$ for which

a $3 \tan x - \sqrt{3} = 0$,

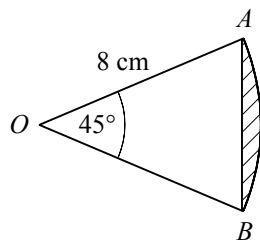
b $2 \cos(x + \frac{\pi}{3}) + \sqrt{3} = 0$.

- 2 Given that $\cos A = \sqrt{3} - 1$,

a find the value of $\sin^2 A$ in the form $p\sqrt{3} + q$ where p and q are integers,

b show that $\tan^2 A = \frac{\sqrt{3}}{2}$.

3



The diagram shows sector OAB of a circle, centre O , radius 8 cm, in which $\angle AOB = 45^\circ$.

- a Find the perimeter of the sector in centimetres to 1 decimal place.

- b Show that the area of the shaded segment is $8(\pi - 2\sqrt{2}) \text{ cm}^2$.

- 4 Find, to 1 decimal place, the values of θ in the interval $0 \leq \theta \leq 360^\circ$ for which

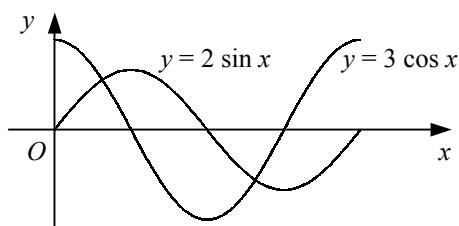
$$2 \sin^2 \theta + \sin \theta - \cos^2 \theta = 2.$$

- 5 Solve, for x in the interval $-\pi \leq x \leq \pi$, the equation

$$3 \sin^2 x = 4(1 - \sin x),$$

giving your answers to 2 decimal places.

6



The diagram shows the curves $y = 2 \sin x$ and $y = 3 \cos x$ for x in the interval $0 \leq x \leq 2\pi$.

Find, to 2 decimal places, the coordinates of the points where the curves intersect in this interval.

- 7 a Sketch the curve $y = \cos 2x^\circ$ for x in the interval $0 \leq x \leq 360$.

- b Find the values of x in the interval $0 \leq x \leq 360$ for which

$$\cos 2x^\circ = -\frac{1}{2}.$$

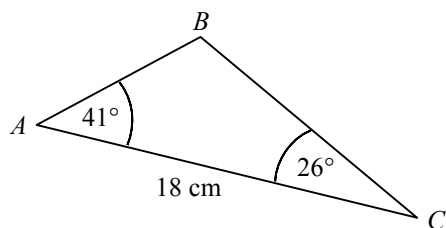
- 8 Solve, for θ in the interval $0 \leq \theta \leq 360$, the equation

$$12 \cos \theta^\circ = 7 \tan \theta^\circ,$$

giving your answers to 1 decimal place.

- 9 Given that $\tan 15^\circ = \frac{\tan 60^\circ - \tan 45^\circ}{1 + (\tan 60^\circ \times \tan 45^\circ)}$,
- a show that $\tan 15^\circ = 2 - \sqrt{3}$,
- b find the exact value of $\tan 345^\circ$.
- 10 Find, to an appropriate degree of accuracy, the values of x in the interval $0 \leq x \leq 360^\circ$ for which $\sin^2 x + 5 \cos x - 3 \cos^2 x = 2$.

11



The diagram shows triangle ABC in which $AC = 18$ cm, $\angle BAC = 41^\circ$ and $\angle ACB = 26^\circ$.

Find to 3 significant figures

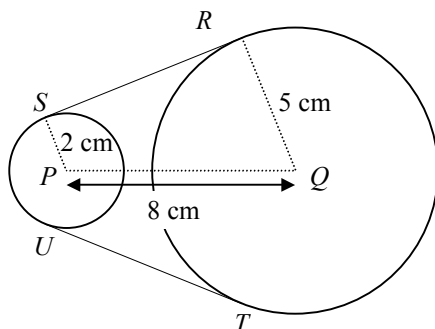
- a the length BC ,
- b the area of triangle ABC .
- 12 Solve, for θ in the interval $0 \leq \theta \leq 360^\circ$, the equation $(6 \cos \theta - 1)(\cos \theta + 1) = 3$.
- 13 Find, in degrees to 1 decimal place, the values of x in the interval $-180^\circ \leq x \leq 180^\circ$ for which $\sin^2 x + 5 \sin x = 2 \cos^2 x$.

14 Prove that

a $\sin^4 \theta - 2 \sin^2 \theta \equiv \cos^4 \theta - 1$,

b $\frac{\sin \theta}{1 + \cos \theta} + \frac{1 + \cos \theta}{\sin \theta} \equiv \frac{2}{\sin \theta}$, for $\sin \theta \neq 0$.

15



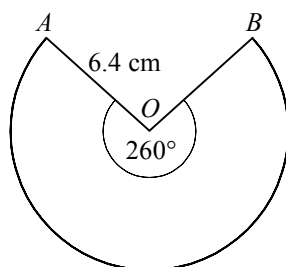
The gears in a toy are shown in the diagram above.

A thin rubber band passes around two circular discs. The centres of the discs are at P and Q where $PQ = 8$ cm and their radii are 2 cm and 5 cm respectively. The sections of the rubber band not in contact with the discs, RS and TU , are assumed to be taut.

- a Show that $\angle PQR = 1.186$ radians to 3 decimal places.
- b Find the length RS .
- c Find the length of the rubber band in this situation.

- 1 Find, in radians to 2 decimal places, the values of θ in the interval $0 \leq \theta \leq 2\pi$ for which
- a $\sin(\theta + \frac{\pi}{4}) = 0.4$, (3)
- b $1 - 3 \cos 2\theta = 0$. (5)
- 2 a Sketch the curve $y = \sin 3x$ for x in the interval $0 \leq x \leq 180^\circ$, showing the coordinates of the turning points of the curve. (3)
- b Solve, for θ in the interval $0 \leq \theta \leq 360^\circ$, the equation
- $$\tan^2 \theta - 2 \tan \theta - 3 = 0. \quad (6)$$

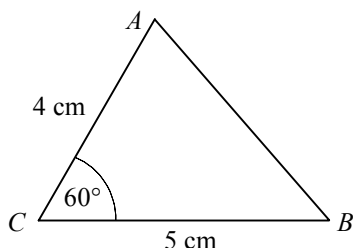
3



The diagram shows the major sector OAB of a circle, centre O , radius 6.4 cm. The reflex angle subtended by the major arc AB at O is 260° .

- a Express 260° in radians, correct to 3 decimal places. (1)
- b Find the perimeter of the major sector OAB . (3)
- c Find the area of the major sector OAB . (2)
- 4 Solve, for θ in the interval $0 \leq \theta \leq 360^\circ$, the equation
- $$3 \cos^2 \theta + 6 \cos \theta = 2 \sin^2 \theta + 6,$$
- giving your answers to 1 decimal place. (7)

5

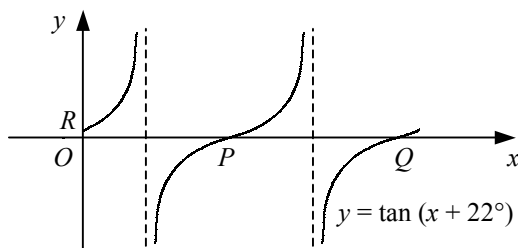


The diagram shows triangle ABC in which $AC = 4$ cm, $BC = 5$ cm and $\angle ACB = 60^\circ$.

- a Find the exact area of triangle ABC . (2)
- b Show that $AB = \sqrt{21}$ cm. (3)
- c Find the value of $\sin(\angle ABC)$ in the form $k\sqrt{7}$ where k is an exact fraction. (3)
- 6 Find, to 1 decimal place, the values of x in the interval $0 \leq x \leq 360$ for which
- $$\tan(2x + 15)^\circ = 2. \quad (6)$$
- 7 Find the values of θ in the interval $0 \leq \theta \leq 360^\circ$ for which
- $$\sin \theta \tan \theta - \cos \theta = 1. \quad (8)$$

- 8 The line with equation $y = 6$ intersects the circle with equation $x^2 + y^2 - 10x - 2y - 3 = 0$ at the points P and Q .
- Find the coordinates of the centre and the radius of the circle. (3)
 - Find the coordinates of the points P and Q . (3)
 - Find the area of the minor segment enclosed by the chord PQ and the circle. (6)
- 9 Find the values of θ in the interval $0 \leq \theta \leq 360^\circ$ for which
- $$5 \sin^2 \theta + 5 \sin \theta + 2 \cos^2 \theta = 0. \quad (8)$$

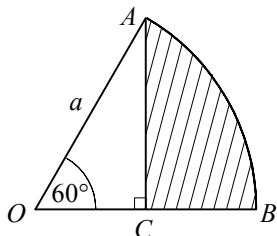
10



The diagram shows the curve $y = \tan(x + 22^\circ)$ for x in the interval $0 \leq x \leq 360^\circ$.

- Write down the coordinates of the points P and Q where the curve crosses the x -axis. (2)
 - Find the coordinates of the point R where the curve meets the y -axis. (1)
 - Write down the equations of the curve's asymptotes. (2)
- 11
- Find, to 1 decimal place, the values of x in the interval $0 \leq x \leq 360^\circ$, for which
- $$5 \sin x = 2 \cos x. \quad (4)$$
- Solve, for y in the interval $0 \leq y \leq 2\pi$, the equation
- $$2 \sin^2 y - \sin y = 1,$$
- giving your answers in terms of π . (6)
- 12 Solve, for θ in the interval $-180^\circ \leq \theta \leq 180^\circ$, the equation
- $$3 \cos^2 \theta - 5 \cos \theta + 2 \sin^2 \theta = 0,$$
- giving your answers to 1 decimal place. (7)

13



The diagram shows the circular sector OAB , centre O . The point C lies on OB such that AC is perpendicular to OB .

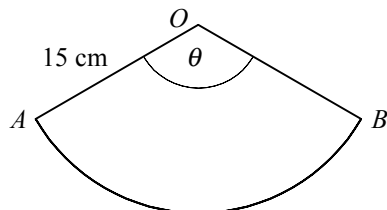
Given that $OA = a$, and that $\angle AOB = 60^\circ$,

- find the area of sector OAB in terms of a and π , (3)
- find the length OC in terms of a , (1)
- show that the area of the shaded region bounded by the arc AB and the straight lines AC and BC is given by $\frac{1}{24} a^2 (4\pi - 3\sqrt{3})$. (5)

- 1 Find, to 1 decimal place, the values of x in the interval $-180^\circ \leq x \leq 180^\circ$ for which
- a** $\cos(x + 40^\circ) = 0.3$, (3)
- b** $2 + \tan 2x = 0$. (5)

- 2 Find, to 1 decimal place, the values of x in the interval $0 \leq x \leq 360$ for which
- $$2 \tan^2 x^\circ - 4 \tan x^\circ + 1 = 0. \quad (6)$$

3



The diagram shows sector OAB of a circle, centre O , radius 15 cm.

Given that $\angle AOB = \theta$ radians and that the length of the arc AB is 32.1 cm,

- a** find the value of θ , (2)
- b** find the area of sector OAB . (2)

- 4 Solve, for x in the interval $0 \leq x \leq \pi$, the equation

$$\sin\left(2x - \frac{\pi}{3}\right) = \frac{1}{2},$$

giving your answers in terms of π . (6)

- 5 **a** Given that $\sin A = 1 - \sqrt{2}$, show that $\cos^2 A + 2 \sin A = 0$. (4)

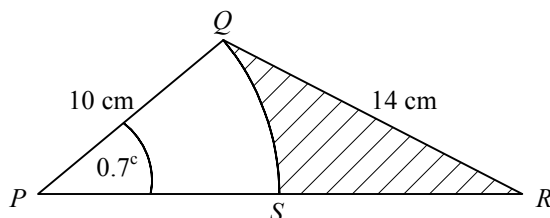
- b** Sketch the curve $y = \sin\left(x + \frac{\pi}{3}\right)$ for x in the interval $0 \leq x \leq 2\pi$.

Label on your sketch

- i** the value of x at each point where the curve intersects the x -axis,
- ii** the coordinates of the maximum and minimum points of the curve. (5)

- 6 Find the values of x in the interval $0 \leq x \leq 360^\circ$ for which
- $$2 \sin^2 x + \sin x + 1 = \cos^2 x. \quad (8)$$

7



The diagram shows triangle PQR in which $PQ = 10$ cm, $QR = 14$ cm and $\angle QPR = 0.7$ radians.

- a** Find the size of $\angle PRQ$ in radians to 2 decimal places. (3)

The point S lies on PR such that $PS = 10$ cm. The shaded region is bounded by the straight lines QR and RS and the arc QS of a circle, centre P .

- b** Find the area of the shaded region. (6)

- 8 a Given that $0 < A < 90^\circ$, and that $\sin A = \frac{\sqrt{5}}{3}$,
- show that $\cos A = \frac{2}{3}$,
 - find the exact value of $\tan A$. (5)

- b Find the values of x in the interval $0 \leq x \leq 360^\circ$ for which
- $$5 \sin x \cos x + \cos x = 0. \quad (6)$$

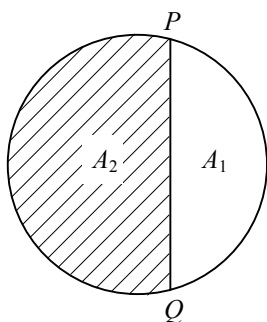
- 9 Find the values of θ in the interval $0 \leq \theta \leq 180$ for which
- $$\cos(2\theta + 30)^\circ = -\frac{1}{2}. \quad (6)$$

- 10 a Sketch the curve $y = \cos(x - 30)^\circ$ for x in the interval $-180 \leq x \leq 180$, showing the coordinates of any maximum or minimum points on the curve. (4)

- b Find the x -coordinates of the points where the curve intersects the line $y = 0.2$ in this interval, giving your answers to 1 decimal place. (3)

- 11 Find the values of x in the interval $0 \leq x \leq 360^\circ$ for which
- $$4 \cos^2 x - \cos x - 2 \sin^2 x = 0. \quad (8)$$

12



The diagram shows a circle of radius r cm. The chord PQ divides the circle into the unshaded minor segment of area A_1 and the shaded major segment of area A_2 .

Given that PQ subtends an angle of θ radians at the centre of the circle,

- a find an expression for A_1 in terms of r and θ . (3)

Given also that $\theta = \frac{5\pi}{6}$,

- b show that $A_1 : A_2 = (5\pi - 3) : (7\pi + 3)$. (6)

- 13 Find, in terms of π , the values of x in the interval $0 \leq x \leq 2\pi$ for which
- $$3 \tan x - 2 \cos x = 0. \quad (7)$$

- 14 In triangle ABC , $AB = 5$ cm, $AC = 7$ cm and $BC = 8$ cm.

- a Find the value of $\cos(\angle ABC)$. (3)

- b Show that the area of triangle ABC is $10\sqrt{3}$ cm². (5)

- 15 a Show that

$$(2 + \cos^2 \theta)(1 + \tan^2 \theta) \equiv 3 + 2 \tan^2 \theta. \quad (3)$$

- b Hence find the values of θ in the interval $0 \leq \theta \leq 360^\circ$ for which

$$(2 + \cos^2 \theta)(1 + \tan^2 \theta) = 7. \quad (5)$$